Reg. No. : $\qquad$
Name : $\qquad$

# Second Semester B.Sc. Degree Examination, December 2021 

First Degree Programme Under CBCSS

## Statistics

Complementary Course for Mathematics

## ST 1231.1 - PROBABILITY AND RANDOM VARIABLES

 (2018 and 2019 Admission)Time : 3 Hours
Max. Marks : 80

## SECTION - A

Answer all questions, each question carries 1 mark.

1. Define sample space of a random experiment with suitable example.
2. When will you say that several events are mutually exclusive and exhaustive?
3. Mention any two drawbacks of the classical definition of probability.
4. State multiplication theorem of probability.
5. Define a priori probability.
6. Distinguish between discrete and continuous random variables.
7. Find the value of $a$, if a random variable $X$ had $\operatorname{pdf} f(x)=a e^{-\frac{x}{5}}, x>0$.
8. For two random variables $X$ and $Y$, show that $E(X+Y)=E(X)+E(Y)$
9. Show that the first central moment of a random variable is always zero.
10. Show by an example that the moment generating function of a random variable does not exist always.

$$
\text { (10 } \times 1=10 \text { Marks })
$$

## SECTION - B

Answer any eight questions, each question carries 2 marks.
11. Seven balls are distributed in two bags at random. What is the probability that the first bag contains 4 balls?
12. If two unbiased dice are thrown, what is the probability that the product of the outcomes is a prime number?
13. If $A$ and $B$ are mutually exclusive events and $P(A)=\frac{1}{3}$ and $P(B)=\frac{1}{4}$, find the values of $P(\bar{A} \cap B)$ and $P(\bar{A} \cup B)$.
14. Show that if two events $A$ and $B$ are independent, $P(A \cap B)=P(A) P(B)$
15. Show that pairwise independence does not imply mutual independence, with the help of an example.
16. A bag contains 3 oranges and 2 apples and another bag contains 4 oranges and 3 apples. A bag is selected at random and one fruit is drawn from the selected bag. What is the probability that the selected fruit is an orange?
17. Define the distribution function of a random variable. What are its important properties?
18. The joint pdf of two random variables $X$ and $Y$ is

$$
f(x, y)=\frac{1}{27}(x+2 y), x=0,1,2 ; y=0,1,2
$$

Find the marginal density functions of $X$ and $Y$.
19. If a random variable $X$ has $p d f f(x)=e^{x}, x>0$, find the distribution of $Y=3 X$.
20. Show that $\mu_{2}=\mu_{2}^{\prime}-\left(\mu_{1}^{\prime}\right)^{2}$ where $\mu_{r}$ represents $r^{\text {th }}$ central moment and $\mu_{1}^{\prime}$ represents the $r^{\text {th }}$ raw moment.
21. Define the conditional expectation $E(X / Y)$.
22. Define the characteristic function of a random variable. What is its advantage over the moment generating function?
( $8 \times 2=16$ Marks)

## SECTION - C

Answer any six questions. Each question carries 4 marks.
23. State and prove addition theorem of probability.
24. A five digit number is formed with digits $0,1,2,3,4$. Find the probability that the number is (a) divisible by 5 (b) an odd number.
25. The probability that a 50 year old man will be alive at 60 is 0.83 and the probability that a 45 year old woman will be alive at 55 is 0.87 . What is the probability that a man, who is 50 and his wife, who is 45 will both alive 10 years hence?
26. State and prove Baye's theorem.
27. Find the value of $k$ such that $f(x)=k x(1-x), 0<x<1$ is a pdf. Also find $P\left[X>\frac{1}{2}\right]$.
28. The joint pdf of two random variables $X$ and $Y$ is given by $f(x, y)=\frac{1}{8}(\overline{6}-x-y)$, $0<x<2,2<y<4$
(a) Find the marginal density functions of $X$ and $Y$
(b) Examine whether X and Y are independent.
29. If $X$ is a random variable with density function $f(x)=\left(\frac{1}{2}\right)^{x}, x=1,2,3 \ldots$, find the pdf of $Y=X^{2}$.
30. Derive the relationship between the $r^{\text {th }}$ central moment and raw moments.
31. When will you say that several random variables are mutually independent? Give an example for mutually independent events.
( $6 \times 4=24$ Marks)

## SECTION - D

Answer any two questions, each question carries 15 marks.
32. (a) Define the term 'Statistical regularity'. How the probability is defined based on this property?
(b) A town has two doctors $A$ and $B$, working independently. The probability that doctor $A$ is available for consultation at a particular time is 0.9 and the doctor $B$ is available with probability 0.8 . What is the probability that at least one doctor is available when needed?
33. (a) Define the conditional probability of events.
(b) For three events $A, B$ and $C$. show that

$$
P(A \cup B / C)=P(A / C)+P(B / C)+P(A \cap B / C)
$$

34. (a) Define probability mass function of a discrete random variable. What are its important properties?
(b) A coin is tossed till the outcome is 'head' and the random variable $X$ dinote the number of tosses. Write the probability mass function of $X$.
35. (a) Show that the moment generating function of the sum of two independent random variables is the product of their moment generating functions.
(b) If a random variable $X$ has pdf $f(x)=\lambda e^{-2 x}, x>0$, find the moment generating function and hence the mean and variance of $X$.
( $2 \times 15=30$ Marks)

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Second Semester B.Sc. Degree Examination, December 2021 First Degree Programme Under CBCSS

## Physics

## Complementary Course for Mathematics

# PY 1231.1 - THERMAL PHYSICS AND STATISTICAL MECHANICS <br> (2020 Admission Regular) 

Time: 3 Hours
Max. Marks : 80

## SECTION - A

Answer all questions in one or two sentences. Each question carries 1 mark.

1. What are the desirable thermal properties of material to be used for constructing cooking utensils?
2. Give an estimate on the temperature of photosphere and core of the sun.
3. Plot the TS diagram of a Carnot's cycle.
4. How does entropy vary in reversible and irreversible processes?
5. What does the second law of thermodynamics represent?
6. Entropy is considered as an extensive property. Why?
7. Why do we call thermal radiation as infrared radiation?
8. Differentiate between isochoric and isobaric processes.
9. What is the main objective of statistical mechanics?
10. What is a pyrheliometer?

$$
\text { ( } 10 \times 1=10 \text { Marks) }
$$

SECTION - B

Answer any eight questions, not exceeding a paragraph. Each question carries 2 marks.
11. Explain the molecular theory for heat conduction.
12. Work out the analogy between black body radiation and a perfect gas.
13. In a furnace, two iron pieces are heated to the same temperature. One piece is then taken out. Which piece will appear brighter just at this instant? Explain.
14. Draw the blackbody spectrum for three temperatures with emissive power as a function of wavelength.
15. Distinguish between closed and isolated systems with example.
16. Give the important properties of entropy.
17. How does the internal energy of a system develop?
18. List the significances and limitations of first law of thermodynamics.
19. Draw the PV diagram for a diesel engine.
20. Mention the important characteristics of heat engine cycles.
21. Make a comparison on reversible and irreversible processes.
22. Show that for the whole system on which the Carnot engine operates, the algebraic sum of the entropy changes for the whole cycle is zero.
23. Explain why adiabatic compression causes heating.
24. What is a phase space?
25. What are the assumptions made in stating Rayleigh Jean's law?
26. What is a black body? What are its characteristics?
( $8 \times 2=16$ Marks )
SECTION - C

Answer any six questions. Each question carries 4 marks.
27. Distinguish between thermometric conductivity and thermal conductivity.
28. Thermal conductivity of brass is 4 times of copper. Two bars, one of brass and the other of copper of same length and same cross sectional area are joined together. The free ends of copper and brass are kept at steam point and ice point respectively. Find the temperature of the joint in the condition of steady state. Heat loss due to radiation is neglected.
29. Calculate the work done when one litre of monatomic perfect gas at NTP is compressed adiabatically to half its volume. $\gamma=1.66$.
30. Show that there is no change in entropy for reversible cycle.
31. For a Diesel engine, find the adiabatic compression ratio if the combustion expansion ratio is 4 . Given the efficiency of the engine as $52.0 \%$ and $\gamma=1.4$.
32. Calculate the average energy of Planck's oscillator for $(h \omega / \mathrm{KT})=0.01,0.1,1.0$ and 10.0 .
33. The solar radiation with maximum energy is found to be at 490 nm If the Wien's constant is 0.002898 , find the temperature of the sun. Also find the temperature of the moon, if the $14 \mu \mathrm{~m}$ radiations are the most intense from the moon.
34. Compare the ensembles.
35. Prove that the adiabatic curve is steeper than the isothermal curve at a point where the two curves intersect each other.
36. The electrical conductivity of a copper wire of length 500 m and diameter 0.2 mm at room temperature is $5.9 \times 10^{7} \Omega^{-1} \mathrm{~m}^{-1}$. Find its thermal conductivity if the Lorentz number is $2.32 \times 10^{-8} \mathrm{~W}^{2} \mathrm{~K}^{-2}$.
37. A wooden ice box of 1.8 cm thick, lined inside with cork 4 cm thick. If the temperature of the inner surface of the cork is $0^{\circ} \mathrm{C}$ and that of the outer surface of wood is $10^{\circ} \mathrm{C}$, what is the temperature of the interface? The thermal conductivity of wood is $0.12 \mathrm{Wm}^{-1} \mathrm{~K}^{-1}$ and that of cork is $0.037 \mathrm{Wm}^{-1} \mathrm{~K}^{-1}$.
38. Show that the value of $v_{x}$ is $(4.6 \mathrm{kT} / \mathrm{m})^{0.5}$ for which the probability falls to 0.1 times the maximum value.

$$
(6 \times 4=24 \text { Marks })
$$

## SECTION - D

Answer any two questions. Each question carries 15 marks.
39. Discuss the Lee's disc method for finding the conductivity of bad conductors.
40. Derive the expressions for the work done during isothermal and adiabatic processes. Distinguish between adiabatic and isothermal elasticities.
41. Explain the energy distribution in black body radiation. Discuss the success and limitations of the classical theory in explaining it. Derive Planck's radiation formula and explain how it overcomes the short comings of the classical theory.
42. Briefly describe the Maxwell Boltzmann energy distribution and velocity distribution laws.
43. With necessary theory describe the working of petrol engine. Derive the expression for its efficiency.
44. Establish the relation between the second law of thermodynamics and entropy. Analyse the entropy change when ice is converted into steam.

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\text { ( } 2 \times 15=30 \text { Marks })
$$

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Second Semester B.A./B.Sc./B.Com. Degree Examination, December 2021. First Degree Programme under CBCSS

Language Course - English

## EN 1212.1/EN 1211.2/ EN 1211.3 - ENGLISH GRAMMAR USAGE AND WRITING

(Common for B.A/ B.Sc./ B.Com. and Career Related Group 2(a))

## (2019 Admission)

Time: 3 Hours
Max. Marks : 80
I. Answer all questions each in a word or a sentence.

1. Change the voice in the sentence.

Let them go.
2. Change the sentence "I love eating ice cream" into negative.
3. Supply the question tag for, "You are ok $\qquad$ $\because$.
4. Correct the following sentence.

I write fictions.
5. Begin the following sentence with it.

To write an essay is not easy.
6. Choose the correct verb form.

Trouble $\qquad$ (choose/chose) to follow the politician wherever he went:
7. Identify if the following sentence is grammatically correct or not.

The actor grew up as an only child.
8. Rewrite the sentence using the adverb provided. 1 am sad. (quite)
9. Complete the sentences with the correct option.

They are two __ of the same puzzle. (half/halves)
10. The majority of workers ___ not turned up for the strike. (has/have)
( $10 \times 1=10$ Marks)
II. Answer any eight of the following questions as per instructions:
11. Convert the following into a compound sentence.
(a) I have an interview. I am late for it.
(b) The menagerie is far away. It is flooded.
12. Convert the following into a simple sentence.
(a) He is a cop. It is true.
(b) Gopal is alone. He is still cheerful.
13. Correct the following sentences.
(a) Ritu shaked the pencil.
(b) He gave to me a pen holder.
14. Change the voice.
(a) We must take care of the puppy.
(b) Close the gate.
15. Fill in the blanks using the correct verb given in brackets.
(a) The boy has been ___ (missing/to miss) since last week.
(b) Unicorns -_ only in fairy tales. (exist/existed).
16. Choose the correct usage.
(a) Half the shelf __ (is/are) filled with organic products.
(b) Everyone -_ (has/have) duties.
17. Change into comparative degree:
(a) His bike is as old as mine.
(b) Megha is the brightest student in the class.
18. .Frame a question to get the underlined word as answer.
(a) He is a critically acclaimed novelist.
(b) I am living in Melbourne since last year.
19. Add the correct question tag.
(a) Everyone came to the movie premiere, $\qquad$
(b) Buying a new house is a risky affair, ?
20. Reorder the jumbled sentences.
(a) Stuggling dancer/ been/ // have/a
(b) Went/ hiking trip/ they/ on a
21. Choose the appropriate option to fill in the blanks.
(a) The principal did not intend to discuss it any (further/ farther)
(b) Ravi had done it with the $\qquad$ intentions in mind (best/better).
22. Rewrite into positive sentences.
(a) I hate cooking.
(b) He does not like giving impromptu speeches.

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\text { ( } 8 \times 2=16 \text { Marks })
$$

III. Answer any six, as directed:
23. Write a conversation between two friends on a matter of importance.
24. Expand the following proverb:

A stitch in time saves nine.
25. Prepare a questionnaire to assess the pattern of spending time online among teenagers.
26. Prepare a conversation between a teacher and a student who failed a test paper.
27. Change the following conversation into Reported Speech:

Zain: What are you doing?
Cathy: Trying to prepare a quick lunch.
Zain: Do you need my help?
Cathy: Sure. Prep these ingredients for me!
28. Change the following into passive voice.
(a) You can listen to the new song now.
(b) I saw a Banksy painting for sale at the auction.
(c) Somebody stole my purse.
(d) He gave the correct directions.
29. Fill up using articles:

She has bought ___ new watch for you ___ watch is very expensive. It is $\qquad$ smart watch with latest features and ——— platinum strap.
30. Correct the following sentences.
(a) Good friends is harder to come by these days.
(b) I and you can clean this mess.
(c) She is here since seven days.
(d) He gave the speech herself.
31. Complete using suitable modals.
(a) I leave now, as I have to finish my homework. (should/would)
(b) It ___ rain tomorrow. (may/have)
(c) You —__ deliver the talk now.(must/should)
(d) She __ dance properly. (can/would)

$$
(6 \times 4=24 \text { Marks })
$$

IV. Answer any two of the following:
32. Expand the proverb "A thing of beauty is a joy forever".
33. Write a report on the PTA meeting that took place in your college.
34. Write a short essay on the importance of health care workers during the pandemic.
35. Write a report on the importance of world peace.
( $2 \times 15=30$ Marks)

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Second Semester B.A./B.Sc. Degree Examination, December 2021 First Degree Programme Under CBCSS

Language Course
EN 1211.1 : ABILITY ENHANCEMENT COMPULSORY COURSE: ENVIRONMENTAL STUDIES AND DISASTER MANAGEMENT

## (2020 Admission Regular)

## Time: 3 Hours

Max. Marks : 80
I. Answer all questions, each in a sentence or two. Each question carries 1 mark.

1. What is biodiversity?
2. Why is the air precious to the red man?
3. Define Ecosystem.
4. Which are the two birds who have returned due to trophic cascade?
5. What is identified as a major threat to the conservation of the natural resources and the biodiversity?
6. What is a biodiversity hotspot?
7. What do you mean by environmental pollution?
8. Who is the speaker of the poem "The memory of Hiroshima"?
9. Expand UNISDR.
10. Give the name of the gas leaked out of the UCC plant at Bhopal.

$$
\text { (10 } \times 1=10 \text { Marks) }
$$

II. Answer any eight, each in a paragraph not exceeding 50 words. Each. question carries 2 marks.
11. What is the condition put forth before the "great chief" by the Chief Seattle?
12. According to Tagore, what are the two different kinds of wisdom possessed by Vashishtha and Vishvamitra?
13. Comment on the line ". . I reintroduced myself to myself, this time a mother".
14. "It was a spring without voices". Explain.
15. Describe the narrator's plot of land.
16. Suggest a few measures to reduce plastic pollution.
17. What is meant by "zero waste philosophy"?
18. Explain the concepts "Native species" and "Relic species".
19. What were the grievances of the villagers hit by the floods?
20. "A relief party came at last". Comment.
21. Who is Tasha?
22. Why was Saku determined to write the best assignment in class?
23. How should one deal with a bomb threat over the phone?
24. What is a man-made disaster? Explain with an example.
25. How did Arif Khan deal with the riotous mob of students?
26. What are the measures taken to ensure proper waste management in the relief camps?
( $8 \times 2=16$ Marks)
III. Answer any six in a paragraph not exceeding 100 words. Each question carries 4 marks.
27. How do the red man's ways differ from those of the white man?
28. Tagore's description of the forest hermitage and the King's court.
29. What are the harmful effects of trophic cascade on the ecosystem?
30. What were the methods tried by the narrator's wife to solve the problem of the bats? Did she succeed?
31. Why is plastic so ubiquitous?
32. How does Satchidanandan present the bleak picture of the Chernobyl disaster?
33. What was Saku's assignment about?
34. Briefly explain the methods to mitigate the adverse impact of floods.
35. Examine the elements of sarcasm in Nissim Ezekiel's poem.
36. Discuss the experiences shared by the survivors of the Bhopal gas tragedy.
37. What is the medical emergency situation faced by Arif Khan? How does he manage to save the life of the person?
38. What are the things to be taken care of while setting up medical camps inside relief camps?
( $6 \times 4=24$ Marks)
IV. Answer any two of the following in not less than $\mathbf{3 0 0}$ words. Each question carries 15 marks:
39. Discuss the ecological concerns and environmental values raised by Chief Seattle in his speech.
40. Explain how Indian Classical literature conceives ecology as mentioned by Tagore.
41. Attempt a critical appreciation of Basheer's story.
42. Gieve Patel's poem voices the anxiety over the mass destruction of trees. Analyse.
43. What is the impact of plastic on the marine eco system?
44. "The Truth about the Floods" reveals the agony of the victims of the floods and the apathy of the officials. Substantiate.

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# Second Semester B.A./B.Sc. Degree Examination, December 2021 First Degree Programme Under CBCSS Language Course : Additional Language - Hindi HN 1211.1 - HINDI NIBANDH AUR ANYA GADYA VIDHAYEN (2020 Admission Regular) 

Time: 3 Hours
I. निर्देश़ : एक शब्द या वाक्य में उत्तर लिखिए।

1. हिन्दी साहित्य के उपन्यास सम्राट कौन है ?
2. 'बडौदा का अनुभव' किस विधा पर लिखी गई रचना है ?
3. द्विवेदी जी के अनुसार देवदार का पुराना नाम क्या है ?
4. मनु भण्डारी कौन है ?
5. 'बेटी का विवाह' किसकी रचना है?
6. तांडद नृत्य का प्रवर्त्तक कौन है ?
7. मणिमधुकर का मूल नाम क्या है?
8. स्वाधीन भारत का संविधान किसने लिखा?
9. हंस पत्रिका के सम्पादक कौन है ?
10. 'निंदा सबद रसाल' किसका कथन है ?

I1. निर्देश : किन्हीं आठ प्रश्नों का उत्तर करीब 50 शब्दों में लिखिए।
11. देवताओं में कौन सबसे बडा ईष्यालू है ? क्यों ?
12. सिराम कौन है? उसे देखकर लेखक को क्या ख्याल आता है ?
13. जीवनी किसे कहते है ?
14. मोबात कौन है ?
15. निंदा रस में किसका चित्रण हुआ है ?
16. 'गेहूँ और गुलाब' में मानव को क्या प्राप्त होता है ?
17. दुष्यंतकुमार को, कमलेश्वर किस पोशाक में बदमाश लगते थे?
18. पारसी व्यवस्थापक ने अम्बेडकर को पहले सराय में ठहरने क्यों नहीं दिया?
19. 'क' के बारें में लेखक ई क्या राय है?
20. प्रेमचन्द ने अपनी बेटी को क्यों नहीं पढाया?
21. संस्मरण किसे कहते हैं?
22. गाँव में हाकिमों की जीपें क्यों आती थी?
23. शिवजी का ध्यान भंग होने पर क्या हुआ?
24. लडकी का ब्याह जल्दी नहीं किया जाए तो समाज क्या-क्या टिप्पणियाँ करती है ?
25. अम्बेडकर को बडौडा में रहने के लिए कहाँ जगह मिली ?
26. राजेन्द्र यादव द्वारा रचित किन्हीं चार रचनाओं के नाम लिखिए।
'III. निर्देश : किन्हीं छ: प्रश्नों के उत्तर करीब $\mathbf{1 2 0}$ शब्दों में लिखिए।
27. लेखक के अनुसार देवदारु महावृक्ष नहीं है। कारण स्पष्ट कीजिए।
28. कन्यादान के प्रति मुंशी प्रेमचन्द का क्या अभिप्राय है ?
29. लेखक की पडोसिन की बीमारी कैसे सुधर गई ?
30. सिराम की तीसरी पत्नी का चित्रण कीजिए।
31. अम्बेडकर भारत लौटकर सीधे बडौदा क्यों आये?
32. 'हाँ हर कहानीकार को कही-न-कहीं शूठ को साधना पडता है' भाव समझाइए।
33. गेहूँ और गुलाब की प्रतीकात्मकता पर प्रकाश डालिए।
34. राजेन्द्र यादव की दृष्टि से कमलेश्वर कैसा व्यक्ति है ?
35. मुंशी भवानी प्रसाद के चरित्र पर प्रकाश डालिए।
36. हजारी प्रसाद द्विवेदी के अनुसार मनोवैज़ानिक और कला समीक्षक कौन-कौन है ?
37. दिसावर और मऊ का अन्तर स्पष्ट कीजिए।
38. रामवृक्ष बेनीपुरी के अनुसार राक्षसता क्या है?
( $6 \times 4=24$ Marks)
IV. निर्देश : किन्हीं दो प्रश्नों के उत्तर 250 शब्दों में लिखिए।
39. 'बेटी का विवाह' जीवनी पर प्रकांश डालिए।
40. 'मेरे हमदम मेरे दोस्त : कमलेश्वर' पाठ की समीक्षा कीजिए।
41. 'निंदा रस' का सारांश लिखिए।
42. 'सूखे सरोवर का भूगोल' में चित्रित गाँव और ग्रामवासियों का चित्रण कीजिए।
43. ‘गेहूँ बनाम गुलाब’ निबंध पर प्रकाश डालिए।
44. 'बडौदा का अनुभव' पाठ में अभिव्यक्त छुआछूत पर प्रकाश डालिए।

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\text { ( } 2 \times 15=30 \text { Marks })
$$

Reg. No. :
Name : $\qquad$

Second Semester B.Sc. Degree Examination, December 2021 First Degree Programme Under CBCSS Mathematics

Foundation Course - II
MM 1221 : FOUNDATIONS OF MATHEMATICS
(2018 \& 2019 Admission)
Time: 3 Hours
Max. Marks : 80

## SECTION - I

All the first ten questions are compulsory. They carry 1 mark each.

1. What is antecedent in a conditional statement?
2. Define tautology.
3. Give the negation of " $S$ is compact and convex."
4. Express the statement "If $x$ is greater than 1 , then $x^{2}$ is greater than 1 " using quantifiers.
5. Define half-open Intervals.
6. Let $L$ be the length of the curve $x=\ln t, y=\sin t(1 \leq t \leq \pi)$. Find an integral expression for $L$.
7. Write the formula for the area $A$ of the region $R$ enclosed by the polar curve $r=f(\theta)(\alpha \leq \theta \leq \beta)$ and the lines $\theta=\alpha$ and $\theta=\beta$.
8. If $v=<-2,0,1>$ and $w=<3,5,-4>$, the find $w-2 v$.
9. Express $u \times v$ as a determinant.
10. Define trace of a surface in a plane.

## SECTION - II

Answer any eight questions from among the questions 11 to 22. These questions carry 2 marks each.
11. Draw the truth table of the biconditional statement.
12. What are the two types of quantifiers?
13. Prove that $(\sim p \Rightarrow c) \Leftrightarrow p$.
14. Prove that $A \cap(U \backslash B)=A \backslash B$, where $A$, and $B$ be any two sets and $U$ is the universal set.
15. Prove that $(a, b)=(c, d)$ if and only if $a=c$ and $b=d$.
16. Define equivalence relation. Give an example.
17. Eliminate $t$ and establish a relation between $x$ and $y$, given $x=2 t-3, y=6 t-7$.
18. Find the slope of the tangent line to the unit circle $x=\cos t, y=\sin t$ at the point $t=\frac{\pi}{6}$.
19. Find the circumference of a circle having radius ' $a$ ' whose parametric equation is $x=a \cos t, y=a \sin t$.
20. Find the center and radius of the sphere $x^{2}+y^{2}+z^{2}-2 x-4 y+8 z+17=0$.
21. Find a vector that is orthogonal to both of the vectors $u=<2,-1,3>$ and $v=\langle-7,2,-1\rangle$.
22. Calculate the scalar triple product $u .(v \times w)$ of the vectors $u=3 i-2 j-5 k$, $v=i+4 j-4 k, w=3 j+2 k$.

## SECTION - III

Answer any six questions from among the questions 23 to 31 . These questions carry 4 marks each.
23. Prove that $p \Rightarrow q$ and $\sim q \Rightarrow \sim p$ are logically equivalent.
24. Prove that "For every $\varepsilon>0$ there exists $\delta>0$ such that $1-\delta<x<1+\delta \Rightarrow 5-\varepsilon<2 x+3<5+\varepsilon$ ".
25. Let $f(x)$ be an integrable function. If $\int_{0}^{1} f(x) \neq 0$, then prove that there exists an $x$ in $[0,1]$ such that $f(x) \neq 0$.
26. Sketch the trajectory over the time interval $0 \leq t \leq 10$ of the particle whose parametric equations of motion are $x=t-3 \sin t, y=4-3 \cos t$.
27. Without eliminating the parameter, find $d y / d x$ and $d^{2} y / d x^{2}$ at $(1,1)$ and $(1,-1)$ on the semicubical parabola given by the parametric equations $x=t^{2}, y=t^{3}$.
28. Sketch the graph of the equation $r=\sin \theta$ in polar coordinates by plotting points.
29. If $u$ and $v$ are nonzero vectors in 2-space or 3 -space, and if $\theta$ is the angle between them, then prove that $\cos \theta=\frac{u v}{\|u\|\|v\|}$.
30. Let $v=\langle 2,3\rangle, \quad e_{1}=\left\langle\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right\rangle, e_{2}=\left\langle-\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right\rangle$. Find the scalar components of $v$ along $e_{1}$ and $e_{2}$ and the vector components of $v$ along $e_{1}$ and $e_{2}$.
31. Find the orthogonal projection of $v=j+j+k$ on $b=2 i+2 j$, and then find the vector component of $v$ orthogonal to $b$.
( $6 \times 4=24$ Marks)

## SECTION - IV

Answer any two questions from among the questions 32 to 35 . These questions carry 15 marks each.
32. Explain in detail, inductive reasoning and proof by counter example using the function $f(n)=n^{2}+n+17$.
33. (a) Prove that the countable union of countable sets is countable.
(b) Prove that the set of all rational numbers is countable.
34. (a) Find the slope of the tangent line to the circle $r=4 \cos \theta$ at the point where $\theta=\pi / 4$.
(b) Find the arc length of the spiral $r=e^{\theta}$ between $\theta=0$ and $\theta=\pi$.
35. (a) Suppose that two forces are applied to an eye bracket. Find the magnitude of the resultant and the angle $\theta$ that it makes with the positive $x$-axis.
(b) Find the angle between a diagonal of a cube and one of its edges.

$$
(2 \times 15=30 \text { Marks })
$$

Reg. No. : $\qquad$
Name : $\qquad$

# Second Semester B.A./B.Sc. Degree Examination, December 2021 <br> First Degree Programme under CBCSS <br> Language Course V - Additional Language - Malayalam <br>  <br> (2018 \& 2019 Admission) 

Time : 3 Hours
Max. Marks : 80









P.T.O.









 வృயாைコロガக．




 வロOுmm？




（ $8 \times 2=16$ Marks ）










 (q) $100^{4}$ ?
( $6 \times 4=24$ Marks $)$








( $2 \times 15=30$ Marks)

Reg. No. : $\qquad$
Name: $\qquad$

# Second Semester B.Sc. Degree Examination, December 2021 First Degree Programme Under CBCSS <br> Statistics <br> Complementary Course for Mathematics <br> <br> ST 1231.1 : PROBABILITY AND RANDOM VARIABLES <br> <br> ST 1231.1 : PROBABILITY AND RANDOM VARIABLES (2020 Admission Regular) 

 (2020 Admission Regular)}

Time: 3 Hours
Max. Marks : 80

## SECTION - A

Answer all questions. Each question carries 1 mark.

1. Define sample space.
2. Define statistical regularity.
3. Prove that $P(\phi)=0$.
4. If $A$ and $B$ are independent, then what is $P(A / B)$ and $P(B / A)$ ?
5. State the multiplication theorem of probability.
6. Define compound probability.
7. Give the definition of the distribution function of a two dimensional random vector.
8. Express variance in terms of conditional variance and conditional expectation.
9. State the linearity property of expectation.
10. Define moment generating function associated with a random variable.

## SECTION - B

Answer any eight questions. Each question carries $\mathbf{2}$ marks.
11. Distinguish between mutually exclusive and exhaustive events with examples.
12. For any two events $A$ and $B$ in the same sample space prove that $P(A \cap B) \leq P(A) \leq P(A \cup B) \leq P(A)+P(B)$.
13. Give the classical definition of probability and mention its drawbacks.
14. Define probability as a 'measure', explaining the term 'measure'.
15. What do you mean a probability space?
16. State the law of total probability.
17. If $A$ and $B$ are independent events then prove that $A$ and $B^{C}$ are independent and $A^{C}$ and $B$ are independent.
18. If $A, B$ and $C$ are mutually independent, then prove that $A \cup B$ and $C$ are independent.
19. If the joint pdf of $X$ and $Y$ is $p(x, y)=\frac{1}{22}(2 x+3 y), x=0,1$ and $y=1,2$ what is the joint distribution function?
20. Find the conditional pdf of $X / Y$, if the joint pdf of $(X, Y)$ is $f(x, y)=2-x-y, 0<x, y<1$.
21. When do you say that two random variables are stochastically independent?
22. Define the concept of Transformation of one dimensional random variables.
23. Show that $E(X)=E(E(X / Y))$, with usual notations.
24. Write the expression for the $r^{\text {th }}$ and $s^{\text {th }}$ product moment about the origin of the bivariate random vector $(X, Y)$.
25. Give the Cauchy-Schwartz inequality.
26. Show that $\phi_{x}(t)$ and $\phi_{x}(-t)$ are complex conjugate functions, where $\phi_{X}(t)$ is the characteristic function of the random variable $X$.

$$
(8 \times 2=16 \text { Marks })
$$

## SECTION - C

Answer any six questions. Each question carries 4 marks.
27. Give the axiomatic definition of probability.
28. Tom speaks truth in 30 percent cases and Jerry speaks truth in 25 percent cases. What is the probability that they would contradict each other?
29. Discuss the frequency/statistical definition of probability. Using this definition, prove that $P\left(A^{C}\right)=1-P(A)$.
30. Suppose $A, B$ and $C$ are events such that $P(A)=P(B)=P(C)=1 / 4, P(A \cap B)=0=P(B \cap C) \quad$ and $\quad P(A \cap C)=\frac{1}{8} . \quad$ Evaluate $P(A \cup B \cup C)$.
31. Each of the three guns has a probability 0.4 of hitting a target. What is the probability that (a) all will hit the target and (b) at least one will hit the target?
32. If $p(x)=c\left(\frac{2}{3}\right)^{x}, x=1,2, \ldots$ is a probability mass function,(a) find $c$ and (b) $P(1<X<3)$.
33. The joint pdf of a two dimensional random variable is $f(x, y)=2,0<x<1 ; 0<y<x$.

Then (a) find the marginal pdfs of $X$ and $Y$ and (b) check whether $X$ and $Y$ are independent
34. A continuous random variable $X$ has the pdf $f(x)=A e^{-x / \theta}, x>0$. (a) Find $A$ and (b) for any two positive integers $s$ and $t$ prove that $P(X>s+t / X>t)=P(X>s)$.
35. If $f(x)=1,0<x<1$, find the pdf of $Y=-2 \log X$.
36. A balanced die is rolled. If a person receives Rs. 10 when he gets an even number and loses Rs. 8 when he gets an odd number, how much money can he expect on an average in the long run.?
37. Let $f(x, y)=8 x y, 0<x<y<1$. Find (a) $E(Y / X)$ and (b) $V(Y / X)$.
38. Mention the important properties of a characteristic function.
( $6 \times 4=24$ Marks )

## SECTION - D

Answer any two questions. Each question carries 15 marks.
39. From a group of 8 children including 5 boys and 3 girls, three children are selected at random. What is the probability that (a) No girl (b) only one girl (c) one particular girl (d) at least one girl (e) More girls than boys are selected?
40. Prove or disprove: Mutual independence of three events implies pairwise independent. Is the converse true? Justify your claim.
41. (a) State and prove Baye's theorem.
(b) Three identical boxes contain two balls each. One has both red, one has one red and one black and the third has two black balls. A person chooses a box at random and takes out a ball. If the ball is red and the probability that the other ball in the box is also red.
42. Let $f(x, y)=\frac{1}{72}(2 x+3 y), x=0,1,2 \& y=1,2,3$ be the joint $p d f$ of $(X, Y)$. Then find (a) the distribution of $X+Y$, (b) the conditional distribution of $X / X+Y=3$ and (c) examine whether $X$ and $Y$ are independent or not.
43. Find the moment generating function of $X$ with $\operatorname{pdf} f(x)=\frac{1}{\theta}, 0<x<\theta$ and 0 elsewhere. Also compute the mean and the first 4 central moments.
44. Let $X$ and $Y$ have the joint pdf $f(x y)=\frac{x+2 y}{18}, x=1,2 ; y=1,2$. Find the coefficient of correlation between $X$ and $Y$.

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\text { ( } 2 \times 15=30 \text { Marks) }
$$

Reg. No. : $\qquad$
Name : $\qquad$

# Second Semester B.Sc. Degree Examination, December 2021. <br> First Degree Programme under CBCSS 

Physics
Complementary Course for Mathematics

## PY 1231.1 - THERMAL PHYSICS AND STATISTICAL MECHANICS

(2018 and 2019 Admission)
Time: 3 Hours
Max. Marks : 80

> PART - A

Answer all questions. Answer should not exceed two sentences.
Each question carries 1 mark.

1. Define the term Microstate with the help of an example.
2. Explain the term grand canonical ensemble.
3. State Clausius statement of second law of thermodynamics.
4. State equipartition of energy theorem.
5. What is diffusion?
6. Explain the term thermodynamic probability.
7. Define coefficient of performance. Is it greater than one? Explain
8. Explain the term Adiabatic Process.
9. What is the unit of entropy?
10. State Zeroth law of thermodynamics.

$$
\text { (10 } \times 1=10 \text { Marks) }
$$

PART - B

Answer any eight questions. Answer should not exceed one small paragraph. Each question carries 2 marks
11. Distinguish between Accessible and Inaccessible Macrostates.
12. Discuss Lee's disc method for finding the coefficient of thermal conductivity for bad conductors.
13. Deduce the expression for work done during isothermal processes.
14. Show that there is always an increase of entropy in an irreversible cycle.
15. What is an indicator diagram? State its importance.
16. What is the effect of pressure on thermal conductivity?
17. Derive the equation for adiabatic elasticity.
18. Explain the concept of entropy and available energy.
19. Explain the term Thermal Diffusivity or thermometric conductivity.
20. Discuss the distribution of energy in the spectrum of black body on the basis of the spectrum obtained in the experiment performed by Lummer and Pringsheim.
21. State the principle of increase of entropy.
22. Mention the physical significance and properties of entropy.
( $8 \times 2=16$ Marks )
PART - C
Answer any six questions. Each question carries 4 marks
23. Calculate the surface temperature of sun and moon if the wavelength corresponding to the maximum intensity of radiations from them are $4235 A^{0}$ and $15 \mu_{m}$ respectively (Wien's constant $\mathrm{b}=.2892 \times 10^{-2} \mathrm{mk}$ )
24. A quantity of air at $27^{\circ} \mathrm{C}$ and at atmospheric pressure is suddenly compressed to half its original volume. Find the final
(a) pressure and
(b) temperature. Given $\gamma=1.4$.
25. Calculate the probability that in tossing a coin 5 times. we get 3 heads and 2 tails.
26. Calculate the radiant emittance of a black body at a temperature of
(a) 400 K
(b) 4000K Given $\sigma=5.672 \times 10^{-8}$ M.K.S. units.
27. When 50 gm of water is heated from 100 C to 900 C , by how much does its entropy change?
28. Compare the radiant emittance of a black body at 20 K and 200 K . Given $\sigma=5.672 \times 10^{-8} \mathrm{~S}$ units.
29. Find the, efficiency of the Carnot's engine working between the steam point and the ice point.
30. A bar of length 30 cm and uniform area of cross section $5 \mathrm{~cm}^{2}$ consists of two halves $A B$ of copper and $B C$ of iron welded together at $B$. The end $A$ is maintained at $200^{\circ} \mathrm{C}$ and the end C at $0^{\circ} \mathrm{C}$. The sides of the bar are thermally insulated. Find the rate of flow of heat along the bar when the steady state is reached. Thermal conductivity of copper is 0.9 and thermal conductivity of iron is 0.12 CGS units.
31. Calculate the increase in entropy of 10 kg of water at $100^{\circ} \mathrm{C}$ when it changes to vapour. Given Latent heat of steam $=540 \mathrm{cal} /$ gram.
( $6 \times 4=24$ Marks)
PART - D

Answer any two questions. Each question carries 15 marks
32. Define solar constant. Describe an experiment to determine the solar constant using a pyrheliometer.
33. Show that the probability of a molecule to have its velocity component between $v_{x}$, and $v_{x}+d v_{x}$ is given by $P\left(v_{x}\right) d v_{x}=\left(\frac{m}{2 \pi k T}\right)^{\frac{1}{2}} e^{\frac{-m v_{x}^{2}}{2 k T}} d v_{x}$.
34. What is T-S diagram? Find the expression for efficiency of a reversible Carnot's engine with the help of T-S diagram.
35. Calculate the work done in a Carnot's Cycle of operations. Deduce the efficiency of a Carnot's engine in terms of the temperatures between which it works.

$$
.(2 \times 15=30 \text { Marks })
$$

Reg. No. : $\qquad$
Name: $\qquad$

Second Semester B.A./B.Sc./B.Com. Degree Examination, December 2021
First Degree Programme Under CBCSS Language Course - English

## EN 1212.1/EN 1211.2/ EN 1211.3: ENGLISH GRAMMAR USAGE AND WRITING

(Common for B.A./B.Sc./B.Com. and Career Related Group 2(a))
(2020 Admission Regular)
Time : 3 Hours
Max. Marks : 80
I. Answer all questions each in a word or a sentence.

1. Change the voice in the sentence.

Let them go.
2. Change the sentence "I love eating ice cream" into negative.
3. Supply the question tag for, "You are ok, $\qquad$ .$"$.
4. Correct the following sentence.

I write fictions.
5. Begin the following sentence with it.

To write an essay is not easy.
6. Choose the correct verb form.

Trouble
(choose/chose) to follow the politician wherever he went.
7. Identify if the following sentence is grammatically correct or not.

The actor grew up as an only child.
8. Rewrite the sentence using the adverb provided. I am sad. (quite)
9. Complete the sentences with the correct option.

They are two $\qquad$ of the same puzzle. (half/halves)
10. The majority of workers $\qquad$ not turned up for the strike. (has/have)

$$
(10 \times 1=10 \text { Marks })
$$

II. Answer any eight of the following questions as per instructions:
11. Convert the following into a compound sentence.
(a) I have an interview. I am late for it.
(b) The menagerie is far away. It is flooded.
12. Convert the following into a simple sentence.
(a) He is cop. It is true.
(b) Gopal is alone. He is still cheerful.
13. Correct the following sentences.
(a) Ritu shaked the pencil.
(b) He gave to me a pen holder.
14. Change the voice.
(a) We must take care of the puppy.
(b) Close the gate.
15. Fill in the blanks using the correct verb given in brackets.
(a) The boy has been ____ (missing/to miss) since last week.
(b) Unicorns only in fairy tales. (exist/existed).
16. Choose the correct usage.
(a). Half the shelf ____ (is/are) filled with organic products.
(b) Everyone -_ (has/have) duties.
17. Change into comparative degree:
(a) His bike is as old as mine.
(b) Megha is the brightest student in the class.
18. Frame a question to get the underlined word as answer.
(a) He is a critically acclaimed novelist.
(b) I am living in Melbourne since last year.
19. Add the correct question tag.
(a) Everyone came to the movie premiere, $\qquad$
(b) Buying a new house is a risky affair, ?
20. Reorder the jumbled sentences.
(a) Struggling dancer/been///have/a
(b) Went/hiking trip/they/on a
21. Choose the appropriate option to fill in the blanks.
(a) The principal did not intend to discuss it any (further/farther)
(b) Ravi had done it with the $\qquad$ intentions in mind (best/better)
22. Rewrite into positive sentences.
(a) I hate cooking.
(b) He does not like giving impromptu speeches.
23. Change into Direct speech.
(a) She said that she had bought a new Audi.
(b) She said that she won the sweepstakes.
24. Change into exclamatory sentence.
(a) The holiday ended with a bang.
(b) It was a great movie.
25. Write a conversation between two friends on a matter of importance.
26. Expand the following proverb:

A Stitch in time saves nine.

$$
(8 \times 2=16 \text { Marks })
$$

III. Answer any six, as directed:
27. Prepare a questionnaire to assess the pattern of spending time online among teenagers.
28. Prepare a conversation between a teacher and a student who failed in a test paper.
29. Change the following conversation into Reported Speech:

Zain: What are you doing?
Cathy: Trying to prepare a quick lunch.
Zain: Do you need my help?
Cathy: Sure. Prep these ingredients for me!
30. Change the following into passive voice.
(a) You can listen to the new song now.
(b) I saw a Banksy painting for sale at the auction.
(c) Somebody stole my purse.
(d) He gave the correct directions.
31. Fill up using articles:

She has bought new watch for you watch is very expensive. It is $\qquad$ smart watch with latest features and —_ platinum strap.
32. Correct the following sentences.
(a) Good friends is harder to come by these days.
(b) I and you can clean this mess.
(c) She is here since seven days.
(d) He gave the speech herself.
33. Complete using suitable modals.
(a) 1 — leave now, as 1 have to finish my homework. (should/would)
(b) It ___ rain tomorrow. (may/have)
(c) You — deliver the talk now. (must/should)
(d) She ——_ dance properly. (can, would)
34. Prepare a questionnaire to analyse the fitness routine of software professionals.
35. Rewrite using the adverbs provided.
(a) He reaches office late. (generally)
(b) Her judgement is on point. (mostly)
(c) I am happy. (quite)
(d) I have no regrets. (usually)
36. Fill up using suitable prepositions.
(a) I go the library every day.
(b) The car fell
 a ditch.
(c) She was popular $\qquad$
(d). He was sitting me on the plane.
37. Fill up using suitable conjunctions.
(a) The room was spic $\qquad$
(b) The child is strong emotional.
(c) Meena forgot whether to stay —___ leave.
(d) Let me know
you reach the destination.
38. Attempt a dialogue between you and your teacher on how effective online exams were during the pandemic period.

$$
(6 \times 4=24 \text { Marks })
$$

IV. Answer any two of the following:
39. Expand the proverb "A thing of beauty is a joy forever".
40. Write a report on the PTA meeting that took place in your college.
41. Write a short essay on the importance of health care workers during the pandemic.
42. Write a report on the importance of world peace.
43. Outline story.

Snake - middle of the night — scared - child scared - called mother - torch light — black rope - child happy - mother relieved.
44. Expand the proverb "A bird in hand is worth two in the bush".

$$
\text { (2 } \times 15=30 \text { Marks) }
$$

Reg. No. : $\qquad$
Name : $\qquad$

## Second Semester B.Sc. Degree Examination, December 2021

 First Degree Programme under CBCSS Mathematics
## Foundation Course II

## MM 1221 : FOUNDATIONS OF MATHEMATICS

 (2020 Admission Regular)Time : 3 Hours
Max. Marks : 80
PART - A

All the first 10 questions are compulsory and each carries 1 mark :

1. Write the negation of the statement
" $M$ is a cyclic subgroup"
2. Indicate whether the statement
" 5 is not prime or 8 is prime" is true or false.
3. Rewrite the statement "There exists a number less than 7 " using $\exists, \forall$ and $\ni$, as appropriate.
4. If $A, B, C$ are subsets of a universal set $U$, then state whether the statement $A \cap(B \cup C)=(A \cap B) \cup(A \cap C)$ is true or false.
5. Write the parametric equation of semicubical parabola.
6. Write the equation of parabola with focus $(p, o)$ and directrix $x=-p$.
7. Which logical connective corresponds to the set relationship $A \subseteq B$ ?
8. Find the dot product of the vectors $\langle 3,5\rangle$ and $\langle-1,2\rangle$.
9. What is the general form of equation of a plane?
10. Describe the surface $z=(x-1)^{2}+(y+2)^{2}+3$.
PART - B

Answer any eight questions from questions 11 to 26 . These questions carry 2 marks :
11. Write the truth table for $p \vee q$.
12. Identify the antecedent and consequent in the statement "If $n$ is an integer, then $2 n$ is an even integer".
13. Provide a counter example to the statement "Every Continuous function is differentiable".
14. Write the contrapositive statement of the statement "continuity is a necessary condition for differentiability".
15. Let $f: A \rightarrow B$ and $g: B \rightarrow C$ be bijective. Then prove that $g \circ f: A \rightarrow C$ is bijective.
16. State the reflection property of parabolas.
17. Determine a rotation angle $\theta$ that will eliminate the $x y$-term in the equation $2 x^{2}+x y+2 y^{2}+x-y=0$.
18. Name the conic for which the set of points whose distance to the point $(2,3)$ is haif the distance to the line $x+y=1$.
19. Find the new coordinates of the point $(2,4)$ if the coordinate axes are rotated through an angle of $\theta=30^{\circ}$.
20. Find the equation of the hyperbola with vertices $(0, \pm 8)$ and asymptotes $y= \pm \frac{4}{3} x$.
21. Find the arc length of the spiral $r=e^{\theta}$ between $\theta=0$ and $\theta=\pi$.
22. Find the parametric equations of the line passing through $(4,2)$ and parallel to $v=\langle-1,5\rangle$.
23. Calculate the scalar triple product $u \cdot(v \times w)$ of the vectors $u=3 \hat{i}-2 \hat{j}-5 \hat{k}$, $v=\hat{i}+4 \hat{j}-4 \hat{k}, w=3 \hat{j}+2 \hat{k}$.
24. Show that $u \times u=0$ for any vector $u$ in 3-space.
25. Find the vector of length 2 that makes an angle of $\frac{\pi}{4}$ with the positive $x$-axis.
26. Find the distance $d$ between the points $(2,3,-1)$ and $(4,-1,3)$.
PART - C

Answer any six questions from questions 27 to 38 . These questions carry 4 marks each :
27. Construct a truth table for the compound statement
$\sim(p \wedge q) \Leftrightarrow[(\sim p) \vee(\sim q)]$
28. Use a truth table to verify that $p \Rightarrow q$ and $\sim q \Rightarrow \sim p$ are logically equivalent.
29. Let $A=\{1,2,3,4\}$ and $B=\{2,4,6\}$ be subsets of the universal set $U=\{1,2,3,4,5,6\}$. Then what is $A \cup B, A \cap B, A \backslash B$ and $U-B$ ?
30. Let $A=\{1,2,3\}$ and $B=\{2,4,6,8\}$. Which of the following relations are functions between $A$ and $B$ ?
(a) $\{(1,2),(2,6),(3,4),(2,8)\}$
(b) $\{(1,4),(3,8)\}$
(c) $\{(1,6),(2,6),(3,2)\}$
(d) $\{(1,8),(2,2),(3,4)\}$.
31. Find the slope of the tangent line to the circle $r=4 \cos \theta$ at the point where $\theta=\frac{\pi}{4}$.
32. Find the area of the region that is inside the cardioid $r=4+4 \cos \theta$ and outside the circle $r=6$.
33. Find an equation of the parabola that is symmetric about the $y$-axis, has its vertex at the origin and passes through the point $(5,2)$.
34. Find the equations of the paraboloid $z=x^{2}+y^{2}$ in cylindrical and spherical coordinates.
35. Find the spherical coordinates of the point that has rectangular coordinates $(x, y, z)=(4,-4,4 \sqrt{6})$.
36. Sketch the graph of the parabola $x^{2}=12 y$.
37. Describe the surface $z=-\left(x^{2}+y^{2}\right)$.
38. The planes $x+2 y-2 z=3$ and $2 x+4 y-4 z=7$ are parallel since their normals $<1,2,-2>$ and $<2,4,-4>$ are parallel vectors. Find the distance between these planes.
PART - D

Answer any two questions from questions 39 to 44 . These questions carry 15 marks each :
39. Find examples of relations with the following properties.
(a) Reflexive, but not symmetric and not transitive.
(b) Symmetric, but not reflexive and not transitive.
(c) Transitive but not reflexive and not symmetric.
(d) Reflexive and symmetric but not symmetric.
(e) Reflexive and transitive but not symmetric.
40. (a) Let $f: A \rightarrow B$ and $g: B \rightarrow C$. Using the ordered pair definition of the composition $g \circ f$, prove that $g \circ f$ is a function and that $g \circ f: A \rightarrow C$.
(b) Find an example of functions $f: A \rightarrow B$ and $g: B \rightarrow C$ such that
(i) $f$ and $g \circ f$ are both injective but $g$ is not injective.
(ii) $g$ and $g \circ f$ are both surjective but $f$ is not surjective.
(iii) $g \circ f$ is bijective but neither $f$ nor $g$ is bijective.
41. (a) Without eliminating the parameter, find $\frac{d y}{d x}$ and $\frac{d^{2} y}{d x^{2}}$ at $(1,1)$ and $(1,-1)$ on the semicubical parabola $x=t^{2}, y=t^{3}(-\infty<t<\infty)$.
(b) In a disastrous first flight, an experimental paper airplane follows the trajectory of a particle :
$x=t-3 \sin t, y=4-3 \cos t(t \geq 0)$
but crashes into a wall at time $t=10$.
(i) At what times was the airplane flying horizontally?
(ii) At what time was it flying vertically?
42. Sketch the graph of $r=\cos 2 \theta$ in polar coordinates, showing step by step the variation of $\theta$ as follows :

$$
\begin{aligned}
& 0 \leq \theta \leq \frac{\pi}{4}, \frac{\pi}{4} \leq \theta \leq \frac{\pi}{2}, \quad \frac{\pi}{2} \leq \theta \leq \frac{3 \pi}{4}, \quad \frac{3 \pi}{4} \leq \theta \leq \pi, \pi \leq \theta \leq \frac{5 \pi}{4}, \quad \frac{5 \pi}{4} \leq \theta \leq \frac{3 \pi}{2} \\
& \frac{3 \pi}{2} \leq \theta \leq \frac{7 \pi}{4}, \frac{7 \pi}{4} \leq \theta \leq 2 \pi
\end{aligned}
$$

43. (a) Find the angle between the vectors $u=\hat{i}-2 \hat{j}+2 \hat{k}$ and $v=-3 \hat{i}+6 \hat{j}+2 \hat{k}$.
(b) Find the angle between a diagonal of a cube and one of its edges.
(c) Let $v\langle 2,3\rangle, e_{1}=\left\langle\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right\rangle$ and $e_{2}=\left\langle-\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right\rangle$. Find the scalar components of $v$ along $e_{1}$ and $e_{2}$ and the vectors components of $v$ along $e_{1}$ and $e_{2}$.
44. (a) Find parametric equations of the line $L$ passing through the points $p_{1}(2,4,-1)$ and $p_{2}(5,0,7)$.
(b) Let $L_{1}$ and $L_{2}$ be the lines
$L_{1}: x=1+4 t, y=5-4 t, z=-1+5 t$
$L_{2}: x=2+8 t, y=4-3 t, z=5+t$

Do the lines intersect?

Reg. No. : $\qquad$
Name: $\qquad$

# Second Semester B.A./B.Sc. Degree Examination, December 2021 First Degree Programme under CBCSS Language Course V - Additional Language - Malayalam <br>  <br> (2020 Admission - Regular) 

Time: 3 Hours
Max. Marks : 80


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(10 $\times 1=10$ Marks)



















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( $2 \times 15=30$ Marks)

